

Semiconductor fundamentals_B

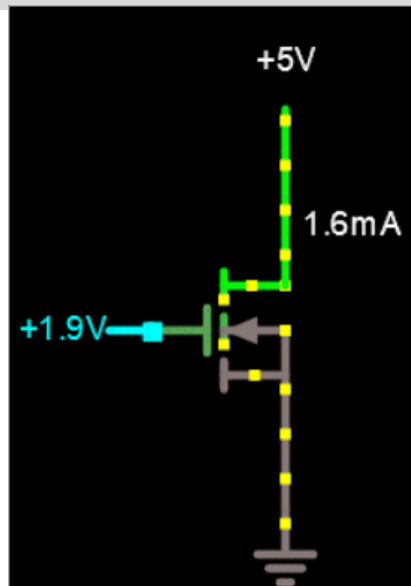
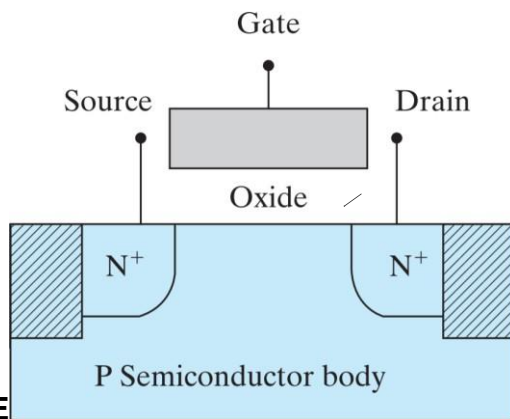
EE302

Prof. Sangyoon Han

Fall 2023

References:

- (C. Hu) Chapter 1
- (R. Pierret) Chapter 1
- Materials from SE393 (Prof. Hongki Kang)



Alternative Expressions for n and p

- Expression of carrier concentration using the intrinsic energy level, E_i
- Assume an intrinsic semiconductor ($E_F = E_i$)

$$- n = n_i = N_C e^{-\frac{E_C - E_i}{kT}}$$

$$- p = n_i = N_V e^{-\frac{E_i - E_V}{kT}}$$

$$- N_C = n_i e^{\frac{E_C - E_i}{kT}}$$

$$- N_V = n_i e^{\frac{E_i - E_V}{kT}}$$

$$n = N_C e^{-\frac{E_C - E_F}{kT}}$$
$$p = N_V e^{-\frac{E_F - E_V}{kT}}$$

$$- n = n_i e^{\frac{E_C - E_i}{kT}} e^{-\frac{E_C - E_F}{kT}} = n_i e^{\frac{E_F - E_i}{kT}}$$

$$- p = n_i e^{\frac{E_i - E_V}{kT}} e^{-\frac{E_F - E_V}{kT}} = n_i e^{\frac{E_i - E_F}{kT}}$$

n_i and the np product

$$n = N_c e^{-(E_c - E_f)/kT} \quad p = N_v e^{-(E_f - E_v)/kT}$$

- Multiplication of n and p ?
- For intrinsic semiconductor ($n = p = n_i$)

$$np = n_i^2$$

Assumptions?

$$n_i = \sqrt{N_c N_v} e^{-E_g/2kT}$$

- n_i is the intrinsic carrier concentration.

$$\left. \begin{array}{ll} n_i \approx 2 \times 10^6/\text{cm}^3 & \text{in GaAs} \\ \approx 1 \times 10^{10}/\text{cm}^3 & \text{in Si} \\ \approx 2 \times 10^{13}/\text{cm}^3 & \text{in Ge} \end{array} \right\} \text{at room temperature}$$

Charge Neutrality Relationship

- **What are the charged entities inside of semiconductors?**
 1. **Electron**
 2. **Hole**
 3. **Ionized donor (+)**
 4. **ionized acceptor (-)**
- **For uniformly doped semiconductor in equilibrium, charge neutrality should satisfy (*why?*)**

Assumes total ionization of dopants

Carrier Concentration Calculations

- **Uniformly doped semiconductor under equilibrium condition**
- **Nondegenerate, Total ionization**

$$np = n_i^2 \quad p - n + N_D - N_A = 0$$

$$\frac{n_i^2}{n} - n + N_D - N_A = 0$$

$$n^2 - (N_D - N_A)n - n_i^2 = 0$$

$$n = \frac{N_D - N_A}{2} + \sqrt{\left(\frac{N_D - N_A}{2}\right)^2 + n_i^2}$$

$$p = \frac{N_A - N_D}{2} + \sqrt{\left(\frac{N_A - N_D}{2}\right)^2 + n_i^2}$$

$$n = \frac{N_D - N_A}{2} + \sqrt{\left(\frac{N_D - N_A}{2}\right)^2 + n_i^2}$$

$$p = \frac{N_A - N_D}{2} + \sqrt{\left(\frac{N_A - N_D}{2}\right)^2 + n_i^2}$$

1. Intrinsic semiconductor

- $N_A = 0$, $N_D = 0$
- $n = n_i$, $p = n_i$

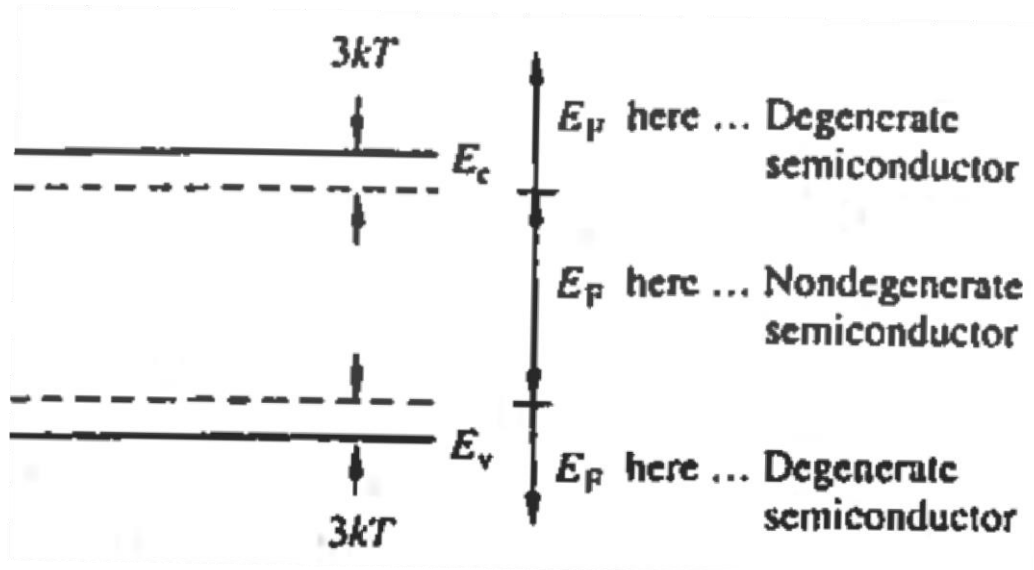
$$n_i \approx 10^{10}/\text{cm}^3 \text{ (Si)}$$

$$N_A \text{ or } N_D > 10^{14}/\text{cm}^3$$

2. Doped semiconductor (mostly one-type, and larger than n_i)

- $(N_D - N_A \approx N_D \gg n_i)$
 - $n = N_D$, $p = n_i^2/N_D$
- $(N_A - N_D \approx N_A \gg n_i)$
 - $n = n_i^2/N_A$, $p = N_A$

Example



- If the semiconductor is in equilibrium and nondegenerate.
- ***What is the hole concentration in an n-type semiconductor with 10^{15} cm^{-3} of donors?***
- ***$n = 10^{15} \text{ cm}^{-3}$***
- ***$p = 10^5 \text{ cm}^{-3}$***

$$n = \frac{N_D - N_A}{2} + \sqrt{\left(\frac{N_D - N_A}{2}\right)^2 + n_i^2}$$

$$p = \frac{N_A - N_D}{2} + \sqrt{\left(\frac{N_A - N_D}{2}\right)^2 + n_i^2}$$

3. Compensated semiconductor

- $N_A =$, $N_D =$
- $n =$, $p =$

4. Doped semiconductor ($n_i \gg |N_D - N_A|$)

- $N_A =$, $N_D =$
- $n =$, $p =$

Determination of E_F (Fermi Level)

$$n = N_c e^{-(E_c - E_f)/kT} \quad p = N_v e^{-(E_f - E_v)/kT}$$

- **First, look at the intrinsic energy level**

- **$n = p$ & $E_F = E_i$**

- $n = N_c e^{-\frac{E_c - E_i}{kT}}, p = N_v e^{-\frac{E_i - E_v}{kT}},$

- $\frac{N_v}{N_c} = \left[\frac{m_p^*}{m_n^*} \right]^{\frac{3}{2}}$

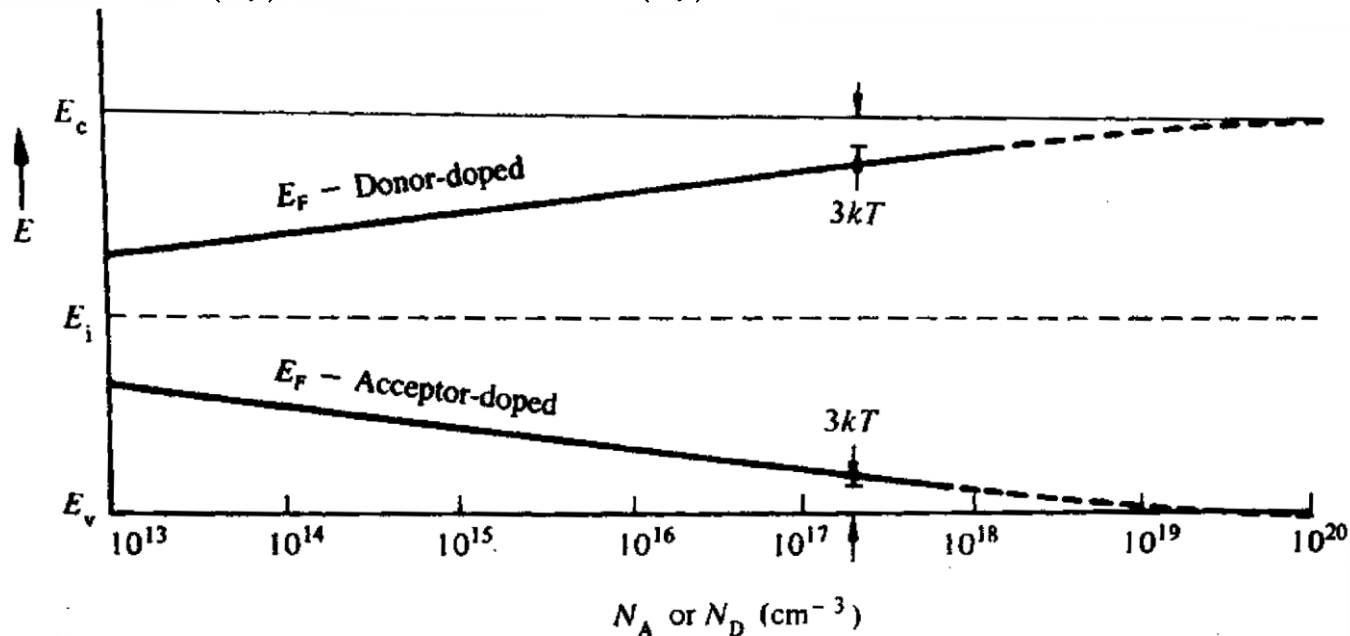
- $E_i = \frac{E_c + E_v}{2} + \frac{3}{4} kT \ln \left(\frac{m_p^*}{m_n^*} \right)$

- **Condition for the intrinsic level to be exactly at the midgap?**

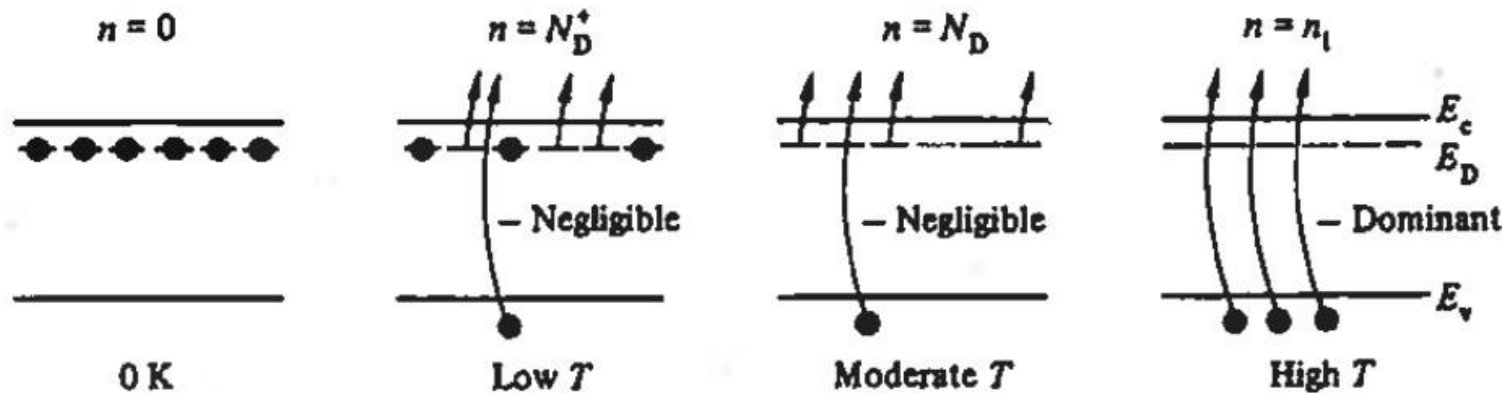
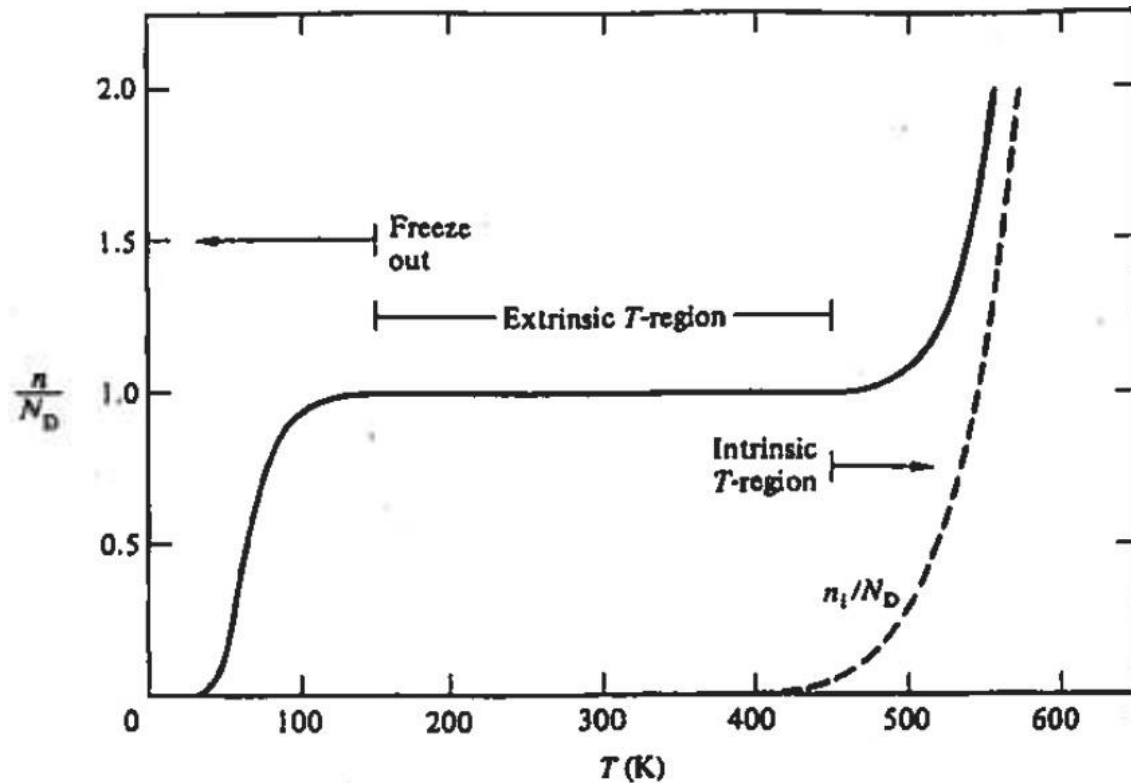
Determination of E_F (Fermi Level)

$$n = n_i e^{\frac{E_F - E_i}{kT}}, \quad p = n_i e^{\frac{E_i - E_F}{kT}}$$

- **Fermi level** in doped semiconductor (nondegenerate, total ionization)
- $E_F - E_i = kT \ln \left(\frac{n}{n_i} \right) = -kT \ln \left(\frac{p}{n_i} \right)$
- $E_F - E_i = kT \ln \left(\frac{N_D}{n_i} \right), \quad E_i - E_F = kT \ln \left(\frac{N_A}{n_i} \right)$

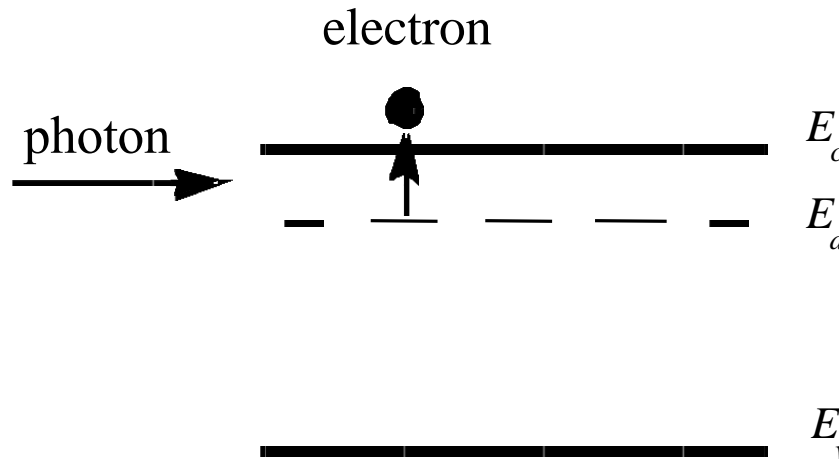


Carrier Concentration Temperature Dependence



Infrared Detector Based on Freeze-out

- To image the black-body radiation emitted by tumors requires a photodetector that responds to $h\omega$'s around 0.1 eV.
- In doped Si operating in the freeze-out mode, conduction electrons are created when the infrared photons provide the energy to ionize the donor atoms.



Summary

- **Studied carriers within a semiconductor under “rest” or equilibrium conditions.**
- **Visualization models**
 - Bonding model
 - Energy band model
- **Carrier concentration → Charge (and the flow of carrier...)**
 - DOS
 - Fermi function
 - Dopant energy levels and concentration
 - Temperature
- **Qualitative and Quantitative understanding of carriers in semiconductor**
 - Which was supposed to be understood by Quantum Mechanics.

Carrier action

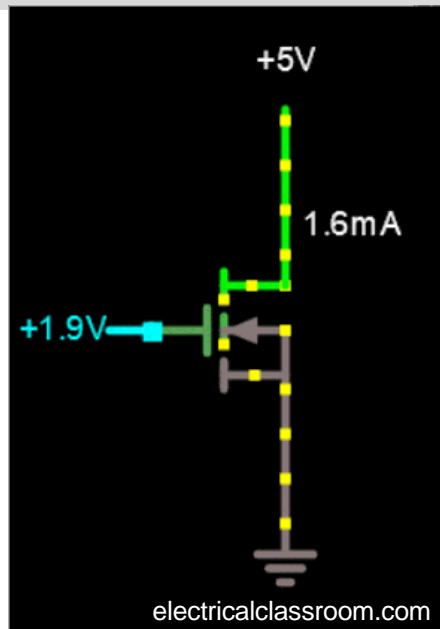
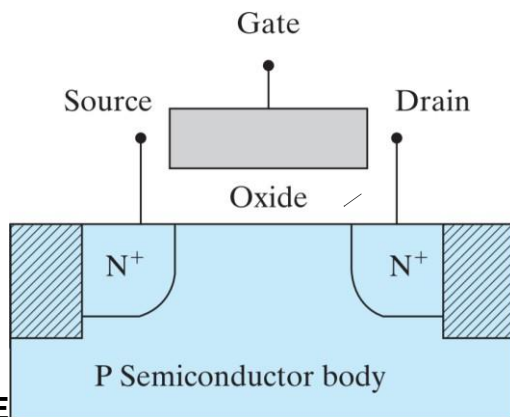
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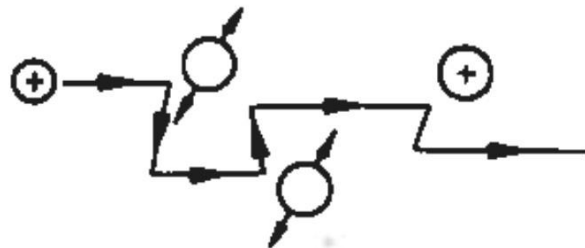
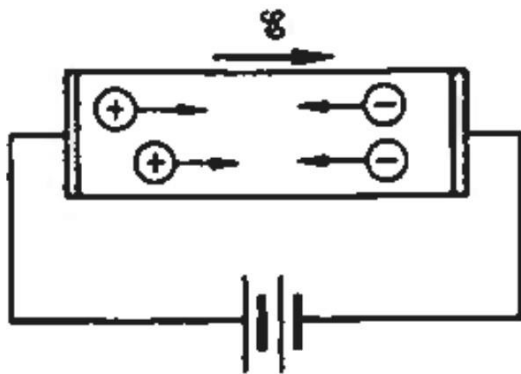
- (C. Hu) Chapter 2
- (R. Pierret) Chapter 3
- Materials from SE393 (Prof. Hongki Kang)



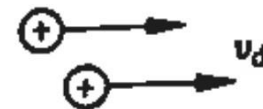
- **Carrier action inside of semiconductor**
 - **Drift**
 - **Diffusion**
 - **Recombination-Generation (R-G)**

- **These contribute to 'non-zero' current components in electronic devices.**

Drift current

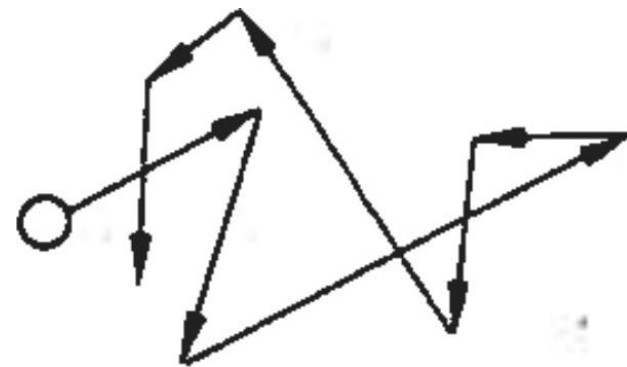


microscopic



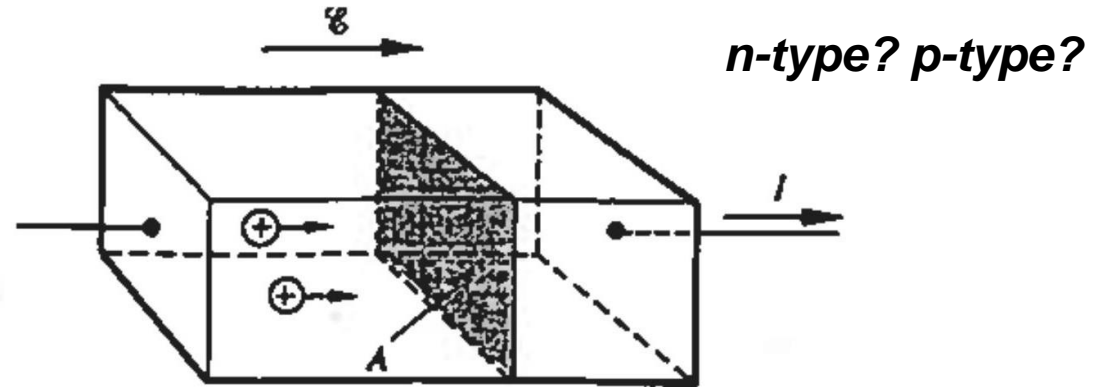
macroscopic

- Drift – *charged* particle motion by applied *electric field*
- Direction for holes and electrons under the same E-field?
- Microscopic
- Macroscopic



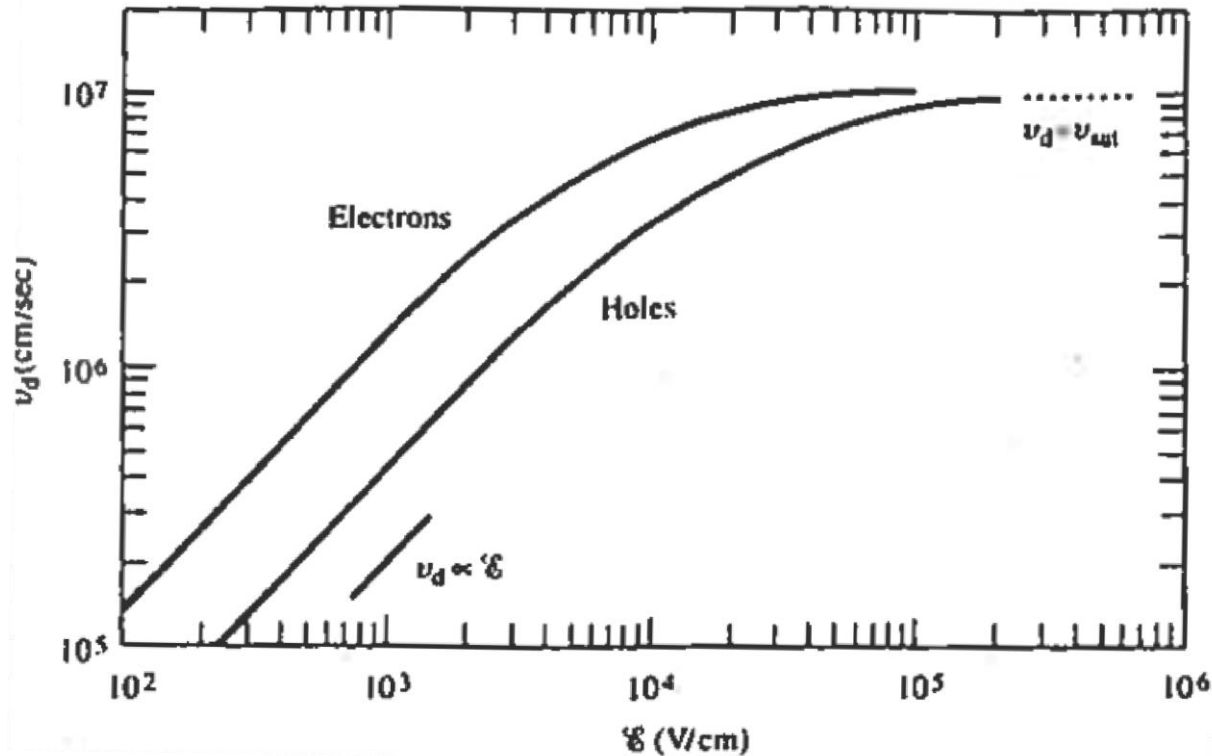
Random thermal motion of carrier

Drift Current



- Current $I = dQ/dt$
- In the perspective of *holes*
 - $v_d t A$ – volume for holes that will cross the plane in a time t
 - $p v_d t A$ – # of holes that will cross the plane in a time t
 - $q p v_d t A$ – amount of charge that will cross the plane in a time t (dq)
 - $I_{P|drift} = q p v_d A$
- Drift current density: $J_{P|drift} = q p v_d$ $J_{N|drift} =$
- Direction?

Drift Velocity



- Relationship between *Electric field* and *Carrier velocity* (n, p)

- $$v_d = \frac{\mu_0 E}{\left[1 + \left(\frac{\mu_0 E}{v_{sat}}\right)^\beta\right]^{\frac{1}{\beta}}}$$

{

(When $E \rightarrow 0$)

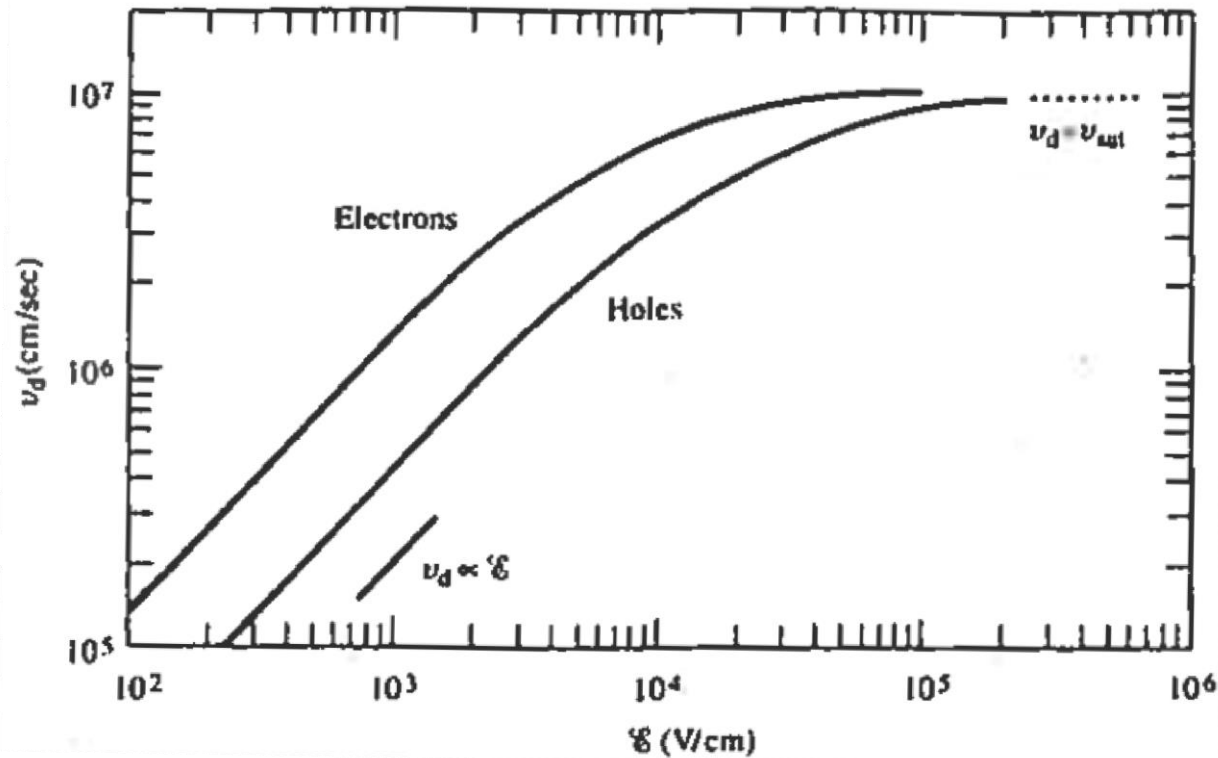
$v_d = \mu_0 E$

}

(When $E \rightarrow \infty$)

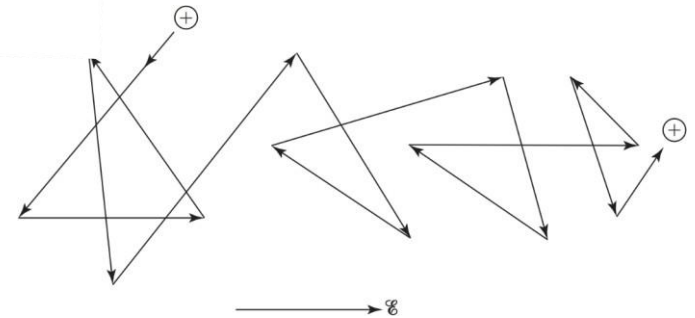
$v_d = v_{sat}$

Drift Velocity saturation (just for your information)




$$m_p v = q E \tau_{mp}$$

$$v = \frac{q E \tau_{mp}}{m_p}$$



- $v_{thermal} \approx \text{speed of light} * \frac{1}{1000}$

Current density

$$v_d = \mu_o E$$


$\mu_p E$ (hole)
 $-\mu_n E$ (electron)

Drift current density:

$$J_{P|drift} = qp v_d \text{ (hole)}$$

$$J_{n|drift} = -qn v_d \text{ (electron)}$$

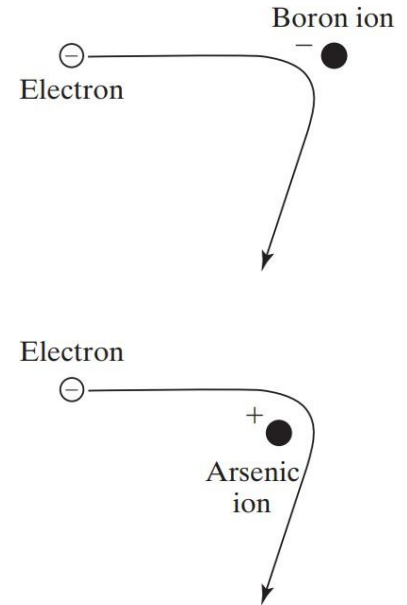
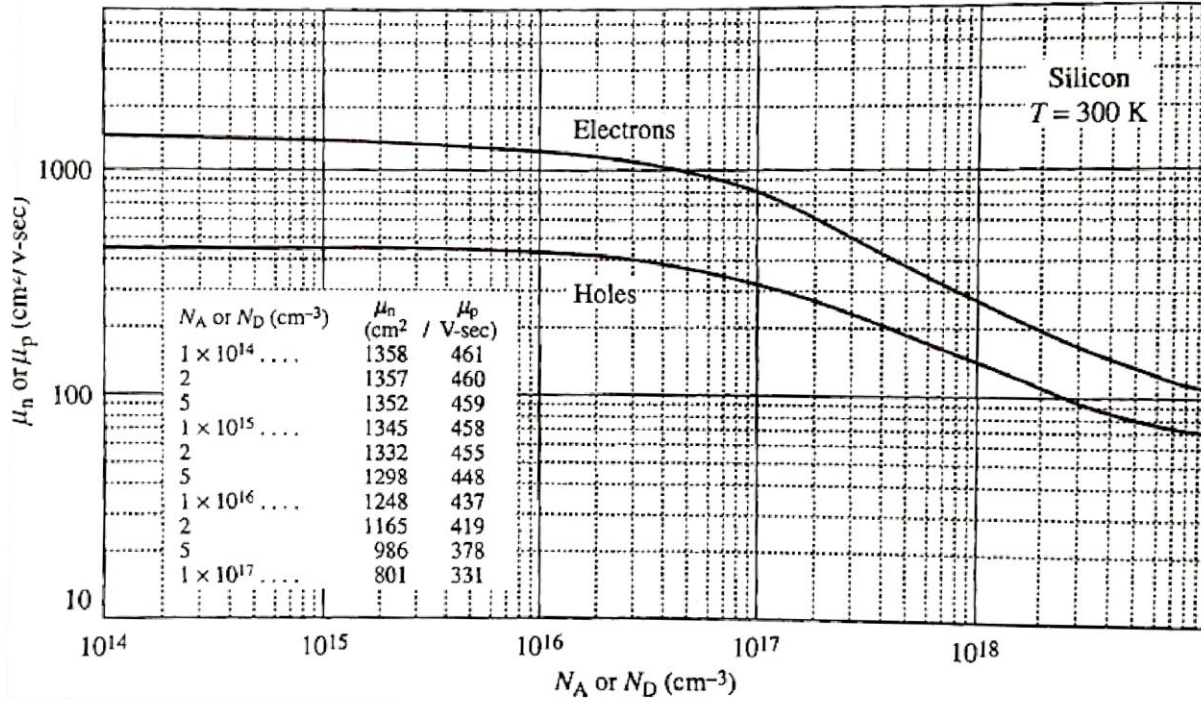
Drift current density:

$$J_{P|drift} = q\mu_p p E \text{ (hole)}$$

$$J_{n|drift} = q\mu_n n E \text{ (electron)}$$

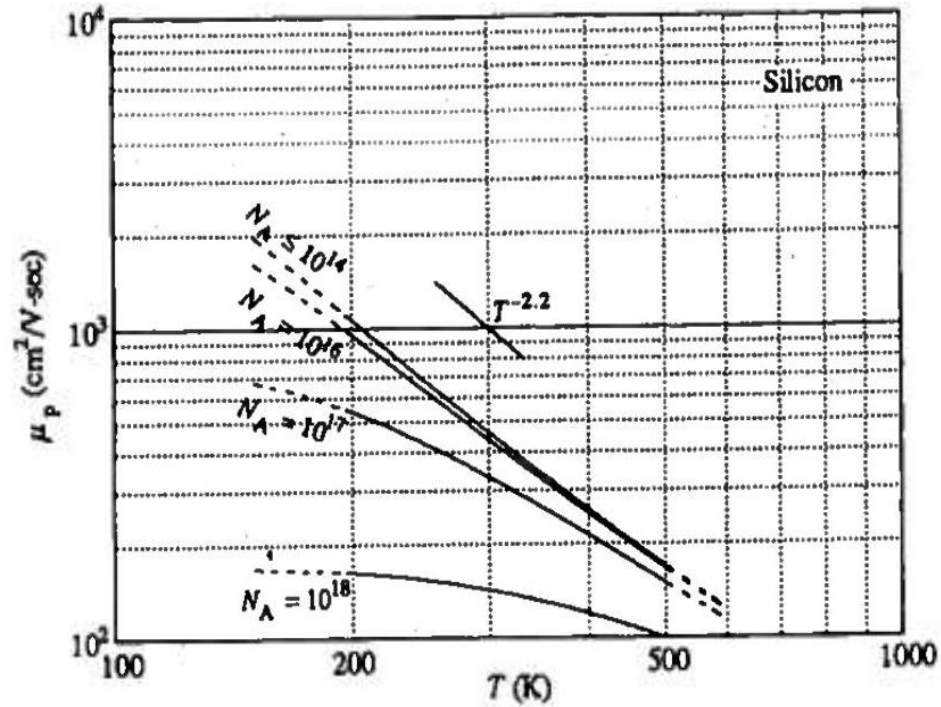
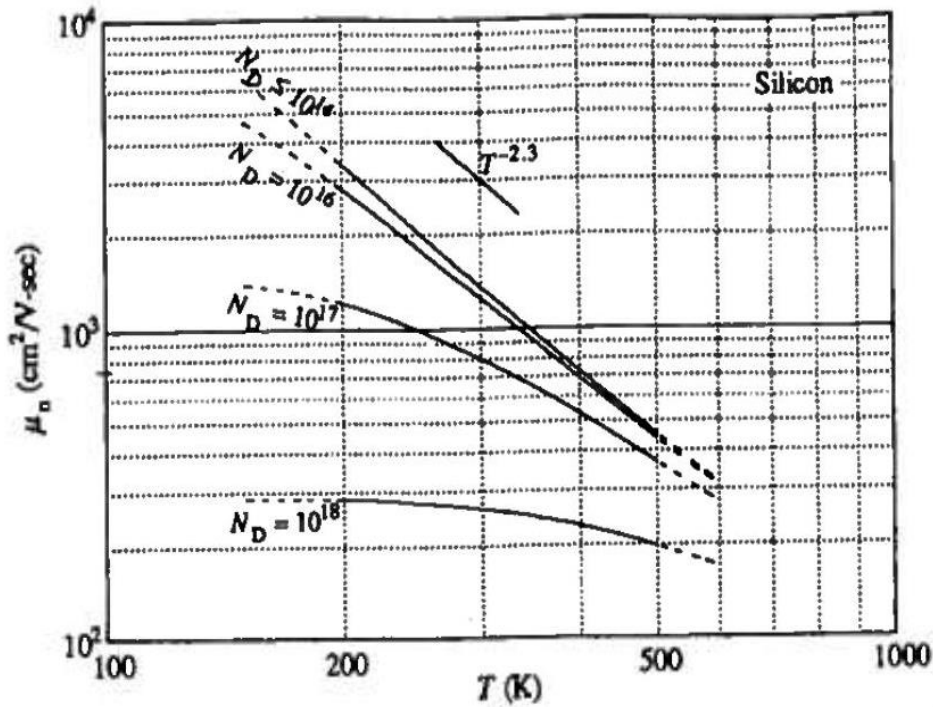
- μ_p \equiv mobility (hole)
- μ_n \equiv mobility (electron)

Mobility (μ)



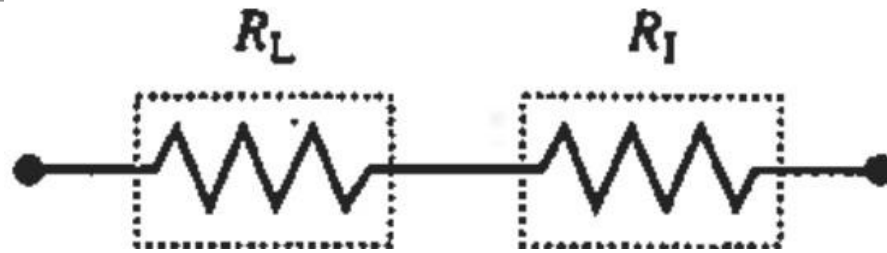
- μ – one of the most representative semiconductor parameter
- Strongly related to *scattering*
 - Doping concentration
 - Temperature (lattice scattering)

Mobility (μ)



- μ – one of the most representative semiconductor parameter
- Strongly related to *scattering*
 - Doping concentration
 - Temperature (lattice scattering)

Mobility (μ)



*Due to
lattice scattering*

*Due to
ionized impurity scattering*

Carrier motion
impedance

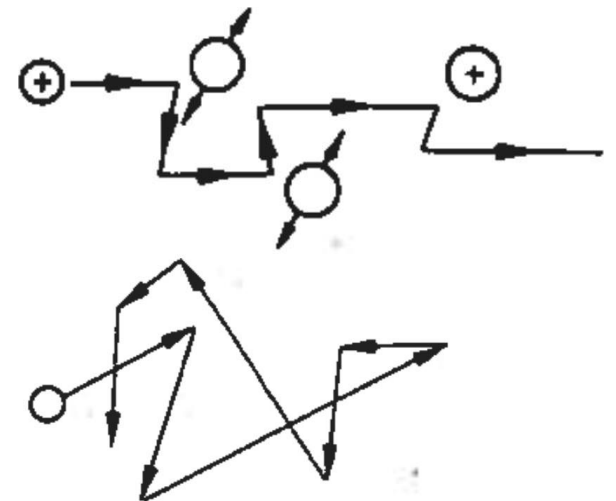
$$R_{total} = R_L + R_I$$

$$\mu = q\langle\tau\rangle/m^*$$

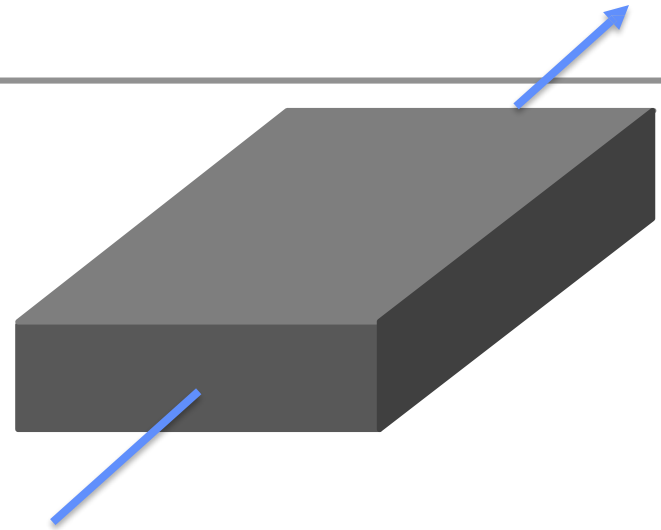
$\langle\tau\rangle$: Mean free time between collisions

m^* : Effective mass for conductivity

- Doping dependence
- Temperature dependence



- Resistivity (ρ) of metal (right)



- How about semiconductor?

- Drift

- Current density, $J = \sigma E$ (σ : conductivity)

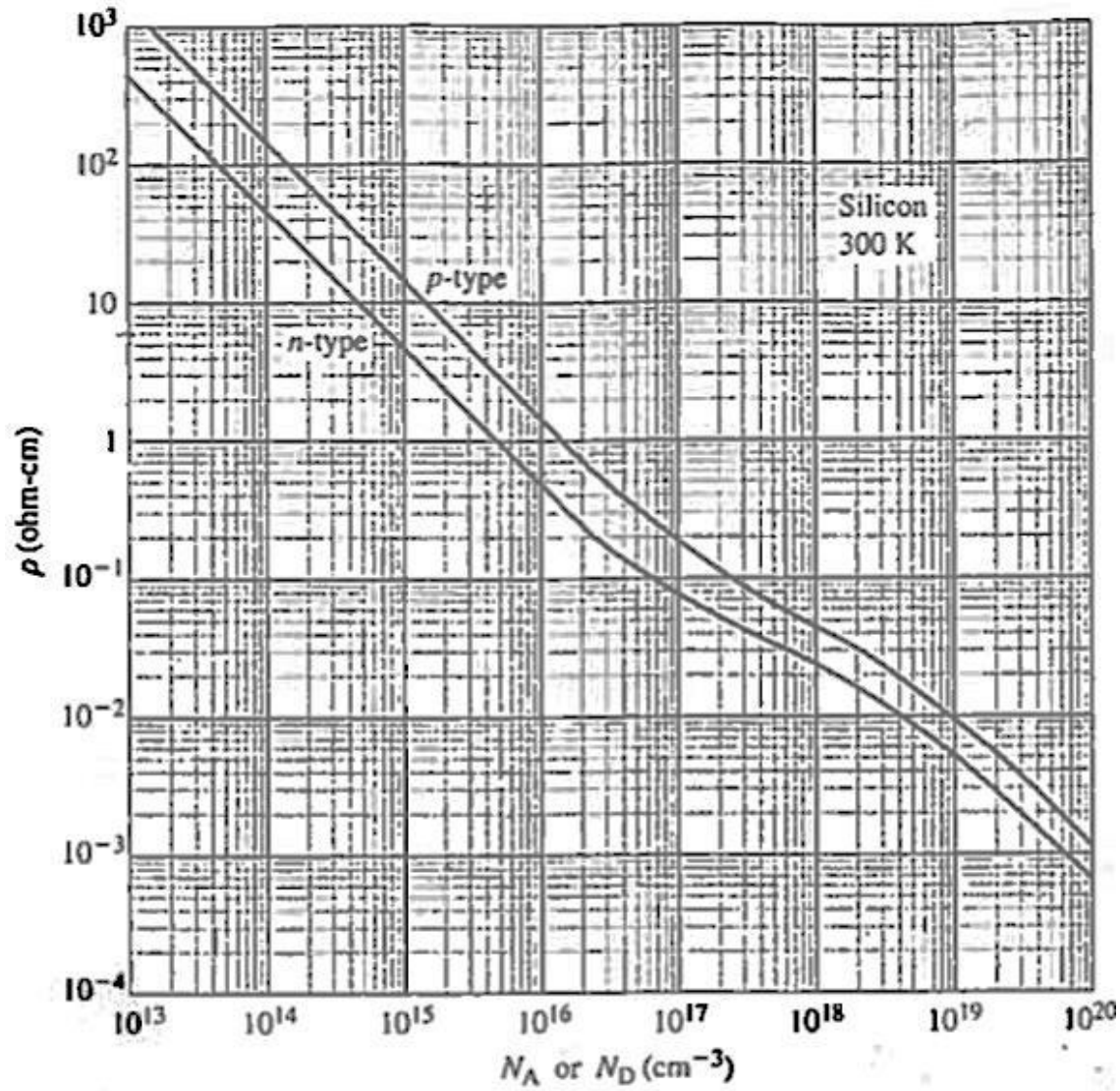
- $E = \left(\frac{1}{\sigma}\right)J = \rho J$ ($\rho = 1/\sigma$: resistivity)

- $J_{drift} = J_{N|drift} + J_{P|drift} = q(\mu_n n + \mu_p p)E$

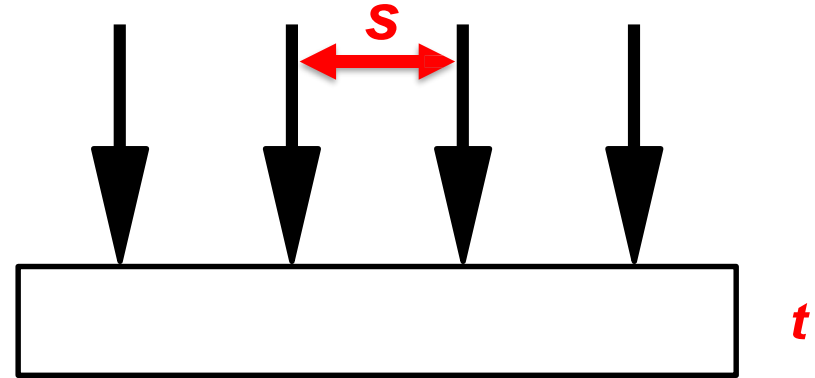
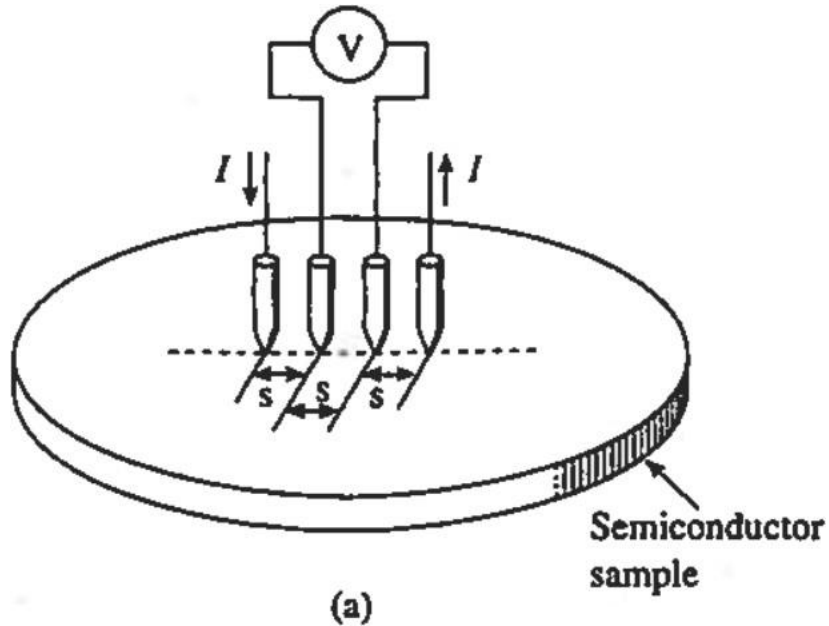
- $\sigma = q(\mu_n n + \mu_p p)$ { (n-type: N_D): $\rho \approx$

- $\rho = 1/q(\mu_n n + \mu_p p)$ { (p-type: N_A): $\rho \approx$

Resistivity



Resistivity (Four-point probe)



- Sample thickness
- Probe spacing (s)

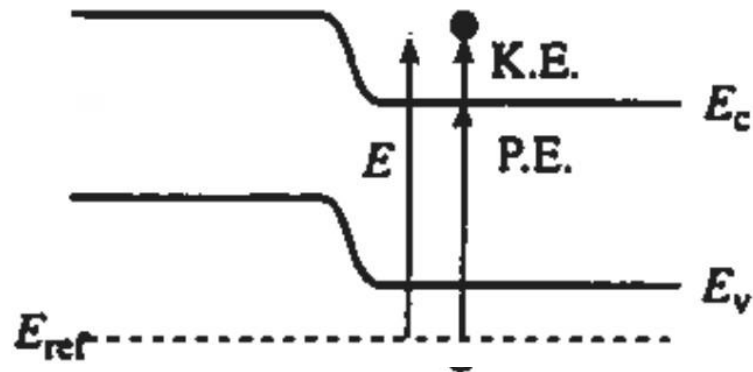
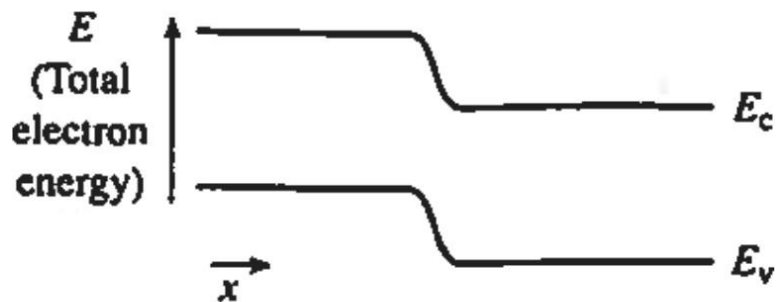
$$\rho = 2\pi s \left(\frac{V}{I} \right) \Gamma$$

$$\Gamma = 1 \quad (t \gg s)$$

$$\Gamma = \frac{t}{2s \ln 2} \quad (t \ll s)$$

Band Bending

- What does band bending mean?



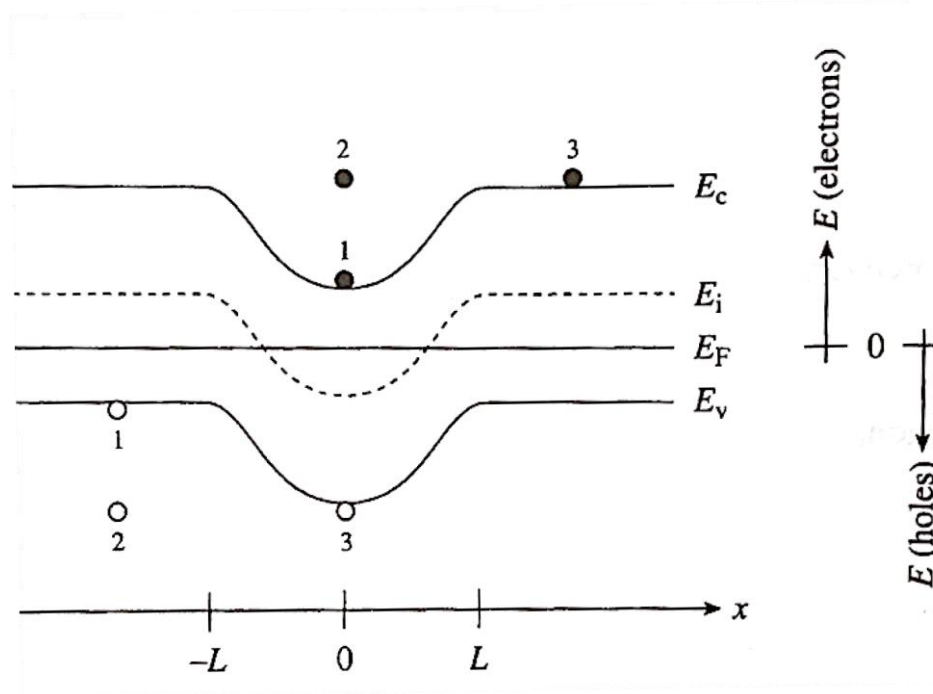
$$\text{Potential Energy} = (-q)V = E_c - E_{ref}$$

$$V = -\frac{1}{q}(E_c - E_{ref})$$

$$E = -\nabla V$$

$$E = \frac{1}{q} \left(\frac{dE_c}{dx} \right) = \frac{1}{q} \left(\frac{dE_v}{dx} \right) = \frac{1}{q} \left(\frac{dE_i}{dx} \right)$$

Band Bending – Example

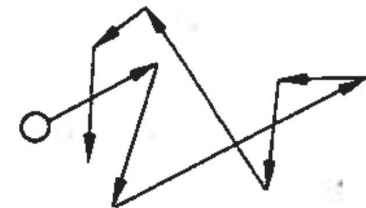
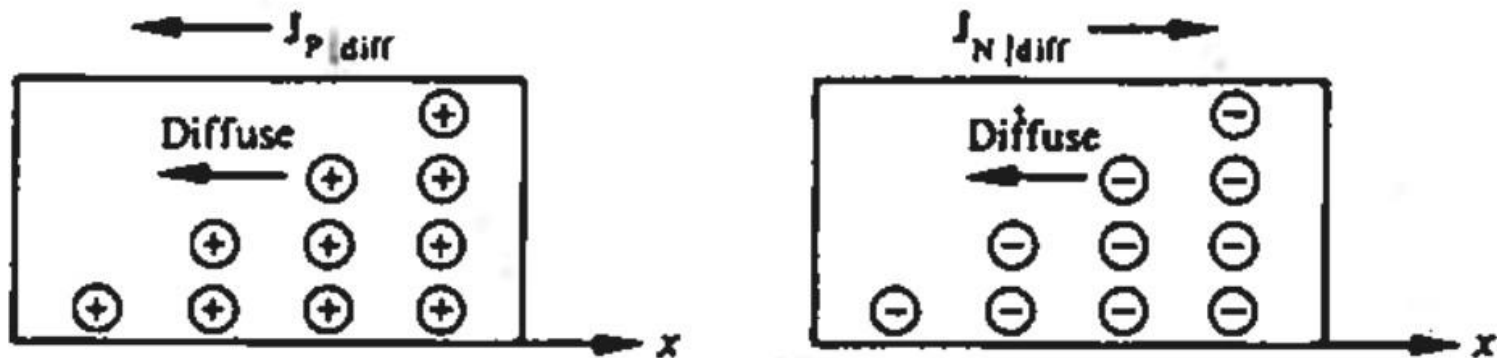


- **Electrostatic potential, $V(x)$?**
- **Electric field, $E(x)$?**

$$E = \frac{1}{q} \left(\frac{dE_c}{dx} \right) = \frac{1}{q} \left(\frac{dE_v}{dx} \right) = \frac{1}{q} \left(\frac{dE_i}{dx} \right)$$

Diffusion current

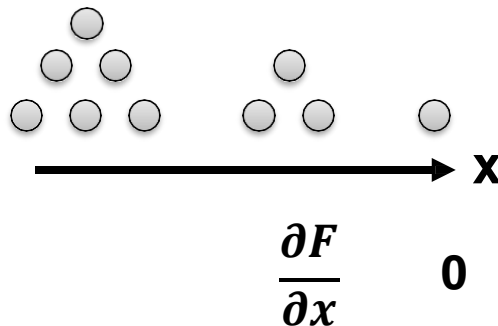
- Diffusion = “Redistribution of carriers by *random thermal motion*”
 - Not by interparticle repulsion
 - Not along different energy states
 - But along locations (over 3D space)
 - *On average*, net movement of carriers from *high* to *low* concentration



Diffusion Currents

- $n(x,y,z)$, $p(x,y,z)$
- $\nabla n \neq 0$, $\nabla p \neq 0$
- **Fick's law (of diffusion)**
 - Flux of particles, F (particles/cm² · sec)
 $F = -D\nabla n$ or $-D\nabla p$
 - D : diffusion coefficient (cm²/sec)
- **Diffusion current density, $J = (\text{charge}) \times (\text{flux})$**
 - $J_{P|\text{diff}} = -qD_p\nabla p$
 - $J_{N|\text{diff}} = qD_n\nabla n$

$$\nabla F = \frac{\partial F}{\partial x} \mathbf{i} + \frac{\partial F}{\partial y} \mathbf{j} + \frac{\partial F}{\partial z} \mathbf{k}$$



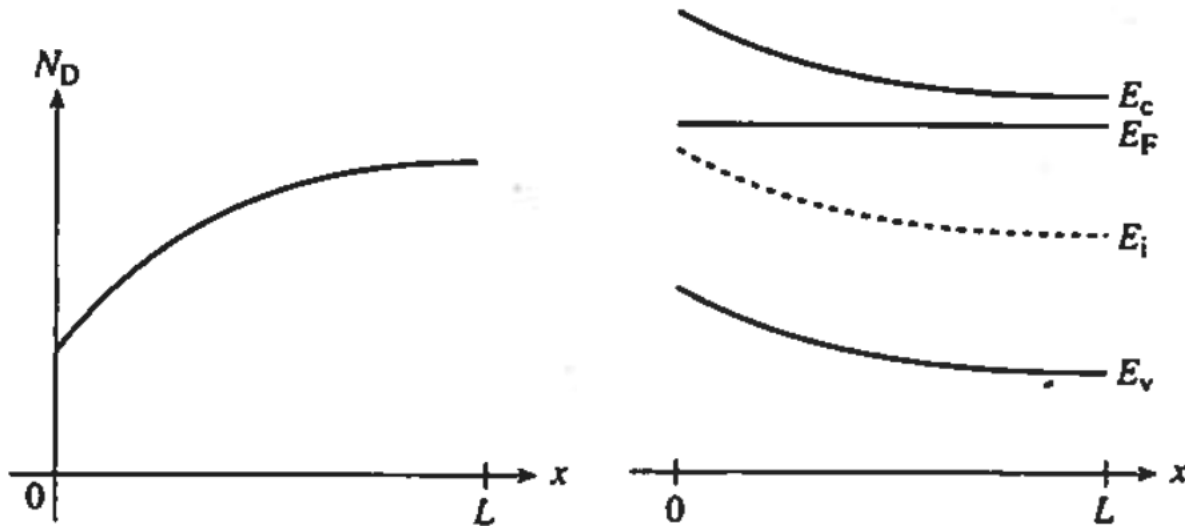
Total Currents

- **Total carrier current: *Drift* + *Diffusion***
 - $J_P = J_{P|drift} + J_{P|diff} = q\mu_p p E - qD_p \nabla p$
 - $J_N = J_{N|drift} + J_{N|diff} = q\mu_n n E + qD_n \nabla n$
 - $J = J_N + J_P$

- **Note that (+/-) sign for drift and diffusion are different.**

Relating Diffusion Coefficients/Mobilities

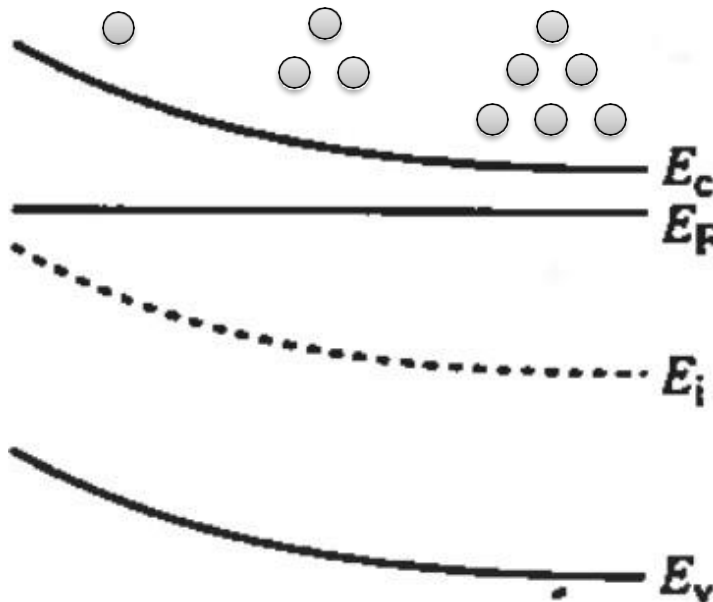
- **Constancy of the Fermi Level**



- **Non-uniformly doped semiconductor**
- **Under equilibrium conditions,**
 - $\nabla E_F = 0; \frac{\partial E_F}{\partial x} = \frac{\partial E_F}{\partial y} = \frac{\partial E_F}{\partial z} = 0$
 - **Fermi level is constant over space.**

Relating Diffusion Coefficients/Mobilities

- Current Flow under Equilibrium Conditions
- Total current in this equilibrium condition must be zero.
- How?



$$E = \frac{1}{q} \frac{dE_i}{dx}$$

$$\begin{aligned} J_N &= J_{N|\text{drift}} + J_{N|\text{diff}} \\ &= q\mu_n n E + qD_n \nabla n \end{aligned}$$

Relating Diffusion Coefficients/Mobilities

- $\mathbf{J}_N = \mathbf{J}_{N|\text{drift}} + \mathbf{J}_{N|\text{diff}} = q\mu_n n \mathbf{E} + qD_n \nabla n = \mathbf{0}$ (under equilibrium)

- $E = \frac{1}{q} \frac{dE_i}{dx}$

- $n = n_i e^{\frac{E_F - E_i}{kT}}$

- $\frac{dn}{dx} =$

- $q\mu_n n \mathbf{E} + qD_n \nabla n = q\mu_n n \mathbf{E} + qD_n \left(-\frac{q}{kT} n \mathbf{E} \right) = \mathbf{0}$

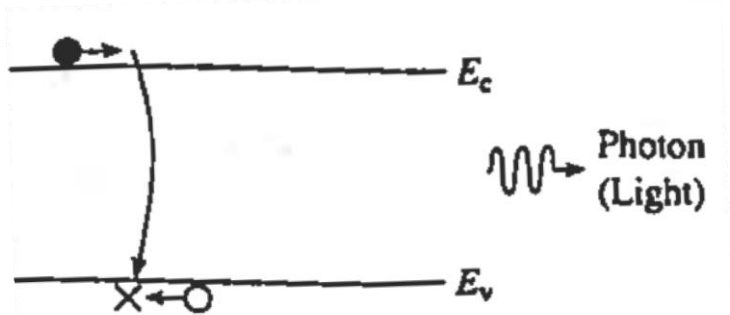
- | |
|------------------------------------|
| $\frac{D_n}{\mu_n} = \frac{kT}{q}$ |
|------------------------------------|

 Einstein Relationship
(it is also valid in *non-equilibrium* condition)

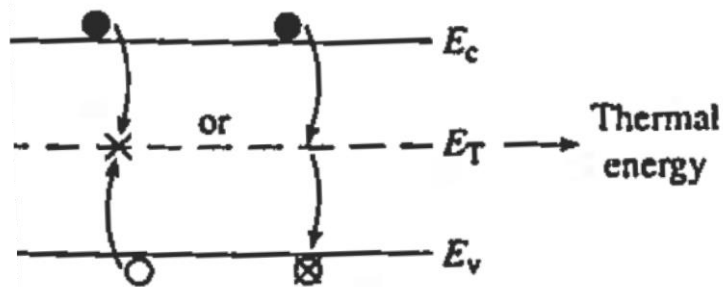
Recombination–Generation

- **Perturbation – Deviation from equilibrium state**
 - Excess or Deficit of carrier concentration from equilibrium values
 - How is the change compensated (or stabilized)?
- **Recombination (R)**
 - A process whereby e^- , h^+ are destroyed (removed).
- **Generation (G)**
 - A process whereby e^- , h^+ are created.
- **When the devices operate, these are mostly in *non-equilibrium* state.**
 - *R-G processes occur by many different mechanisms.*

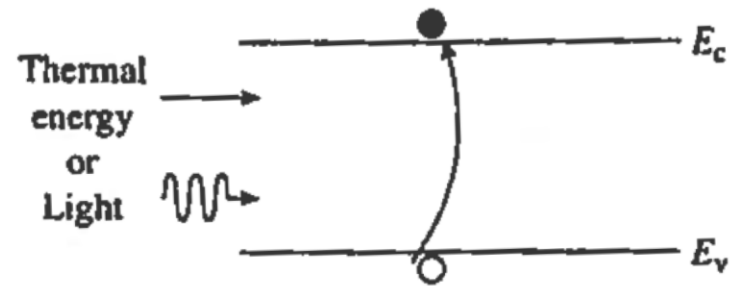
Recombination-Generation



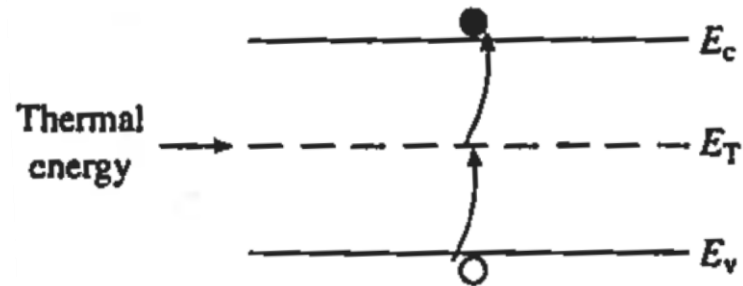
a) Band-to-band recombination



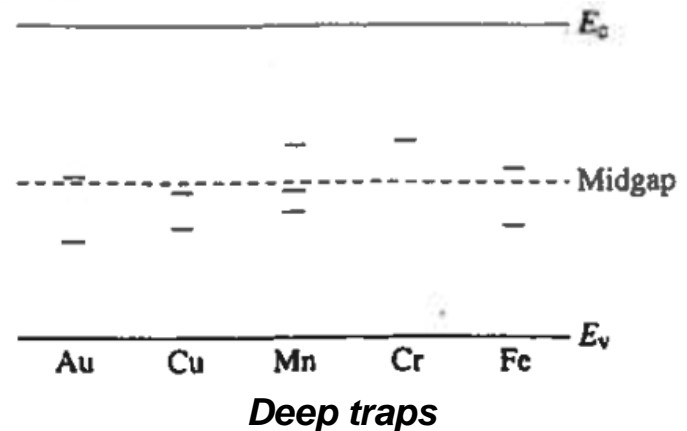
b) R-G center recombination



(d) Band-to-band generation

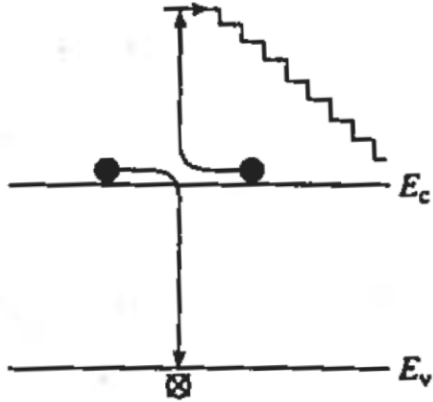


(e) R-G center generation

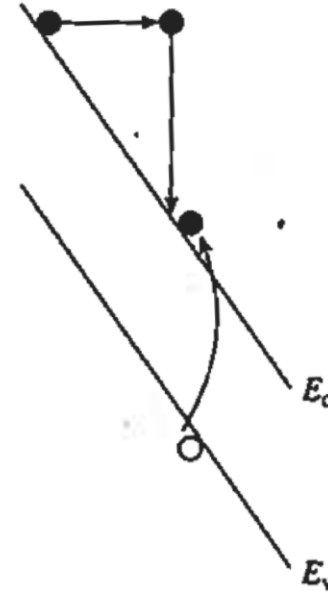


- R-G centers
 - Lattice defects (intrinsic defects)
 - Special impurity atoms \Rightarrow

Recombination–Generation



(c) Auger recombination



(f) Carrier generation via impact ionization

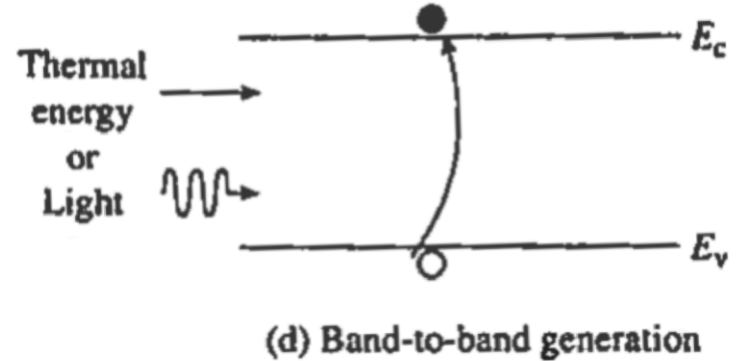
- **Auger recombination**
 - When carrier concentration is high, and thus more collisions occur.
- **Impact ionization**
 - At high E-field & easy to obtain high energy
- **In other conditions, the other mechanism in a previous slide dominates.**

Carrier lifetime (τ)

$$n \equiv n_0 + n'$$

$$p \equiv p_0 + p'$$

$$n' \equiv p' \quad \text{Due to charge neutrality}$$



$$\frac{dn'}{dt} = -\frac{n'}{\tau} = -\frac{p'}{\tau}$$

$$\text{Recombination rate} = \frac{n'}{\tau} = \frac{p'}{\tau}$$

- n' , p' : excess carrier concentrations (e.g. created by light)